## Сумматор Склянского, Radix-16, 16-ти битный

Двоичный Сумматор Склянского, Radix-16, двоичный, 16-ти битный, быстрый (с параллельными операторами С) в виде системы логических уравнений:

```
'--- Step 0 -----
S000 = A0 XOR
                     '1dt
                 в0
C000 = A0 AND
                     '1dt
                в0
S001 = A1 XOR
                в1
                     '1dt
                     '1dt
C001 = A1 AND
                в1
S002 = A2 XOR
                В2
                     '1dt
                     '1dt
C002 = A2 AND
                В2
S003 = A3 XOR
                     '1dt
                в3
C003 = A3 AND
                     '1dt
                в3
                     '1dt
S004 = A4 XOR
                В4
C004 = A4 AND
                в4
                     '1dt
S005 = A5 XOR
                В5
                     '1dt
C005 = A5 AND
                В5
                     '1dt
S006 = A6 XOR

C006 = A6 AND
                 В6
                     '1dt
                     '1dt
                в6
S007 = A7 XOR

C007 = A7 AND
                     '1dt
                 в7
                     '1dt
                в7
S008 = A8 XOR

C008 = A8 AND
                     '1dt
                 в8
                     '1dt
                в8
S009 = A9 XOR
                в9
                     '1dt
C009 = A9 AND
                     '1dt
                в9
S010 = A10 XOR B10
                     '1dt
C010 = A10 AND B10
                     '1dt
                     '1dt
S011 = A11 XOR B11
C011 = A11 AND B11
                     '1dt
S012 = A12 XOR B12
                     '1dt
C012 = A12 AND B12
                     '1dt
S013 = A13 XOR B13
                     '1dt
C013 = A13 AND B13
                     '1dt
S014 = A14 XOR B14
                     '1dt
                     '1dt
C014 = A14 AND B14
S015 = A15 XOR B15
C015 = A15 AND B15
                     '1dt
                     '1dt
'--- Step 1 ------
c100 = c000
                                                      '1dt
C101 = C001 OR_
       S001 AND C000
                                                        '3dt
C102 = C002 OR_
       S002 AND C001 OR_
       S002 AND S001 AND C000
                                                         '3dt
C103 = C003 OR_
       S003 AND C002 OR_
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```
S003 AND S002 AND C001 OR_
        S003 AND S002 AND S001 AND C000
                                                              '3dt
C104 = C004 OR_
        S004 AND C003 OR_
        S004 AND S003 AND C002 OR_
        S004 AND S003 AND S002 AND C001 OR_
        S004 AND S003 AND S002 AND S001 AND C000
                                                          '3dt
C105 = C005 OR
        S005 AND C004 OR_
        S005 AND S004 AND C003 OR_
        S005 AND S004 AND S003 AND C002 OR
        S005 AND S004 AND S003 AND S002 AND C001 OR_
        S005 AND S004 AND S003 AND S002 AND S001 AND C000 '3dt
C106 = C006 OR
        S006 AND C005 OR
        S006 AND S005 AND C004 OR_
        S006 AND S005 AND S004 AND C003 OR_
        S006 AND S005 AND S004 AND S003 AND C002 OR_
        S006 AND S005 AND S004 AND S003 AND S002 AND C001 OR_
        S006 AND S005 AND S004 AND S003 AND S002 AND S001 AND C000 '3dt
C107 = C007 OR_
       S007 AND C006 OR_
S007 AND S006 AND C005 OR_
S007 AND S006 AND S005 AND C004 OR_
       $007 AND $006 AND $005 AND $004 AND $003 OR_

$007 AND $006 AND $005 AND $004 AND $003 AND $002 OR_

$007 AND $006 AND $005 AND $004 AND $003 AND $002 AND $001 OR_

$007 AND $006 AND $005 AND $004 AND $003 AND $002 AND $001 AND
C000 '3dt
C108 = C008 OR_
        S008 AND C007 OR_
        S008 AND S007 AND C006 OR
        S008 AND S007 AND S006 AND C005 OR_
        S008 AND S007 AND S006 AND S005 AND C004 OR
        S008 AND S007 AND S006 AND S005 AND S004 AND C003 OR
        S008 AND S007 AND S006 AND S005 AND S004 AND S003 AND C002 OR_
        S008 AND S007 AND S006 AND S005 AND S004 AND S003 AND S002 AND
C001 OR_
        S008 AND S007 AND S006 AND S005 AND S004 AND S003 AND S002 AND
S001 AND C000 '3dt
C109 = C009 OR_
        S009 AND C008 OR_
        S009 AND S008 AND C007 OR_
        S009 AND S008 AND S007 AND C006 OR_
        S009 AND S008 AND S007 AND S006 AND C005 OR_
        S009 AND S008 AND S007 AND S006 AND S005 AND C004 OR_
S009 AND S008 AND S007 AND S006 AND S005 AND S004 AND C003 OR_
        S009 AND S008 AND S007 AND S006 AND S005 AND S004 AND S003 AND
C002 OR_
        S009 AND S008 AND S007 AND S006 AND S005 AND S004 AND S003 AND
S002 AND C001 OR_
        S009 AND S008 AND S007 AND S006 AND S005 AND S004 AND S003 AND
S002 AND S001 AND C000 '3dt
C110 = C010 OR_{-}
        S010 AND C009 OR_
        S010 AND S009 AND C008 OR_
        S010 AND S009 AND S008 AND C007 OR_
        S010 AND S009 AND S008 AND S007 AND C006 OR_
        S010 AND S009 AND S008 AND S007 AND S006 AND C005 OR_
        S010 AND S009 AND S008 AND S007 AND S006 AND S005 AND C004 OR_
        S010 AND S009 AND S008 AND S007 AND S006 AND S005 AND S004 AND
C003 OR
        S010 AND S009 AND S008 AND S007 AND S006 AND S005 AND S004 AND
S003 AND C002 OR
        S010 AND S009 AND S008 AND S007 AND S006 AND S005 AND S004 AND
S003 AND S002 AND C001 OR_
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```
S010 AND S009 AND S008 AND S007 AND S006 AND S005 AND S004 AND
S003 AND S002 AND S001 AND C000 '3dt
C111 = C011 OR_{-}
       S011 AND C010 OR_
       S011 AND S010 AND C009 OR_
       S011 AND S010 AND S009 AND C008 OR_
       S011 AND S010 AND S009 AND S008 AND C007 OR_
       S011 AND S010 AND S009 AND S008 AND S007 AND C006 OR
       S011 AND S010 AND S009 AND S008 AND S007 AND S006 AND C005 OR_
       S011 AND S010 AND S009 AND S008 AND S007 AND S006 AND S005 AND
C004 OR
       S011 AND S010 AND S009 AND S008 AND S007 AND S006 AND S005 AND
S004 AND C003 OR
       S011 AND S010 AND S009 AND S008 AND S007 AND S006 AND S005 AND
S004 AND S003 AND C002 OR
       S011 AND S010 AND S009 AND S008 AND S007 AND S006 AND S005 AND
S004 AND S003 AND S002 AND C001 OR
       S011 AND S010 AND S009 AND S008 AND S007 AND S006 AND S005 AND
S004 AND S003 AND S002 AND S001 AND C000 '3dt
C112 = C012 OR_
       S012 AND C011 OR_
       S012 AND S011 AND C010 OR_
       S012 AND S011 AND S010 AND C009 OR
       S012 AND S011 AND S010 AND S009 AND C008 OR_
       S012 AND S011 AND S010 AND S009 AND S008 AND C007 OR_
S012 AND S011 AND S010 AND S009 AND S008 AND S007 AND C006 OR_
S012 AND S011 AND S010 AND S009 AND S008 AND S007 AND S006 AND
C005 OR
       S012 AND S011 AND S010 AND S009 AND S008 AND S007 AND S006 AND
S005 AND C004 OR_
       S012 AND S011 AND S010 AND S009 AND S008 AND S007 AND S006 AND
S005 AND S004 AND C003 OR_
       S012 AND S011 AND S010 AND S009 AND S008 AND S007 AND S006 AND
S005 AND S004 AND S003 AND C002 OR
       S012 AND S011 AND S010 AND S009 AND S008 AND S007 AND S006 AND
S005 AND S004 AND S003 AND S002 AND C001 OR_
       S012 AND S011 AND S010 AND S009 AND S008 AND S007 AND S006 AND
S005 AND S004 AND S003 AND S002 AND S001 AND C000 '3dt
C113 = C013 OR_{-}
       S013 AND C012 OR_
       S013 AND S012 AND C011 OR_
       S013 AND S012 AND S011 AND C010 OR_
       S013 AND S012 AND S011 AND S010 AND C009 OR_
       S013 AND S012 AND S011 AND S010 AND S009 AND C008 OR_
       S013 AND S012 AND S011 AND S010 AND S009 AND S008 AND C007 OR_
       S013 AND S012 AND S011 AND S010 AND S009 AND S008 AND S007 AND
C006 OR.
       S013 AND S012 AND S011 AND S010 AND S009 AND S008 AND S007 AND
S006 AND C005 OR_
       S013 AND S012 AND S011 AND S010 AND S009 AND S008 AND S007 AND
S006 AND S005 AND C004 OR_
       S013 AND S012 AND S011 AND S010 AND S009 AND S008 AND S007 AND
S006 AND S005 AND S004 AND C003 OR_
       S013 AND S012 AND S011 AND S010 AND S009 AND S008 AND S007 AND
S006 AND S005 AND S004 AND S003 AND C002 OR_
       S013 AND S012 AND S011 AND S010 AND S009 AND S008 AND S007 AND
S006 AND S005 AND S004 AND S003 AND S002 AND C001 OR_
       S013 AND S012 AND S011 AND S010 AND S009 AND S008 AND S007 AND
S006 AND S005 AND S004 AND S003 AND S002 AND S001 AND C000 '3dt
C114 = C014 OR_{-}
       S014 AND C013 OR_
       S014 AND S013 AND C012 OR_
       S014 AND S013 AND S012 AND C011 OR_
       S014 AND S013 AND S012 AND S011 AND C010 OR_
       S014 AND S013 AND S012 AND S011 AND S010 AND C009 OR_
       S014 AND S013 AND S012 AND S011 AND S010 AND S009 AND C008 OR_
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S014 AND S013 AND S012 AND S011 AND S010 AND S009 AND S008 AND
C007 OR
       S014 AND S013 AND S012 AND S011 AND S010 AND S009 AND S008 AND
S007 AND C006 OR_
       S014 AND S013 AND S012 AND S011 AND S010 AND S009 AND S008 AND
S007 AND S006 AND C005 OR_
       S014 AND S013 AND S012 AND S011 AND S010 AND S009 AND S008 AND
S007 AND S006 AND S005 AND C004 OR
       S014 AND S013 AND S012 AND S011 AND S010 AND S009 AND S008 AND
S007 AND S006 AND S005 AND S004 AND C003 OR_
       S014 AND S013 AND S012 AND S011 AND S010 AND S009 AND S008 AND
S007 AND S006 AND S005 AND S004 AND S003 AND C002 OR_
       S014 AND S013 AND S012 AND S011 AND S010 AND S009 AND S008 AND
S007 AND S006 AND S005 AND S004 AND S003 AND S002 AND C001 OR
       S014 AND S013 AND S012 AND S011 AND S010 AND S009 AND S008 AND
S007 AND S006 AND S005 AND S004 AND S003 AND S002 AND S001 AND C000 '3dt
C115 = C015 OR_
       S015 AND C014 OR_
       S015 AND S014 AND C013 OR_
       S015 AND S014 AND S013 AND C012 OR_
       S015 AND S014 AND S013 AND S012 AND C011 OR_
       S015 AND S014 AND S013 AND S012 AND S011 AND C010 OR_
       S015 AND S014 AND S013 AND S012 AND S011 AND S010 AND C009 OR_
       S015 AND S014 AND S013 AND S012 AND S011 AND S010 AND S009 AND
C008 OR
       S015 AND S014 AND S013 AND S012 AND S011 AND S010 AND S009 AND
S008 AND C007 OR
       S015 AND S014 AND S013 AND S012 AND S011 AND S010 AND S009 AND
S008 AND S007 AND C006 OR
       S015 AND S014 AND S013 AND S012 AND S011 AND S010 AND S009 AND
S008 AND S007 AND S006 AND C005 OR
       S015 AND S014 AND S013 AND S012 AND S011 AND S010 AND S009 AND
S008 AND S007 AND S006 AND S005 AND C004 OR_
       S015 AND S014 AND S013 AND S012 AND S011 AND S010 AND S009 AND
S008 AND S007 AND S006 AND S005 AND S004 AND C003 OR_
       S015 AND S014 AND S013 AND S012 AND S011 AND S010 AND S009 AND
S008 AND S007 AND S006 AND S005 AND S004 AND S003 AND C002 OR
       S015 AND S014 AND S013 AND S012 AND S011 AND S010 AND S009 AND
S008 AND S007 AND S006 AND S005 AND S004 AND S003 AND S002 AND C001 OR_
       S015 AND S014 AND S013 AND S012 AND S011 AND S010 AND S009 AND
S008 AND S007 AND S006 AND S005 AND S004 AND S003 AND S002 AND S001 AND
C000 '3dt
'--- Sum -----
                      '1dt
 S0 = S000
                      '2dt
 S1 = S001 XOR C100
                      '4dt
 S2 = S002 XOR C101
 S3 = S003 XOR C102
                      '4dt
 S4 = S004 \text{ XOR C103}

S5 = S005 \text{ XOR C104}
                      '4dt
                      '4dt
 S6 = S006 \text{ XOR } C105
S7 = S007 \text{ XOR } C106
                      '4dt
                      '4dt
 S8 = S008 XOR C107
                      '4dt
                      '4dt
 S9 = S009 XOR C108
S10 = S010 XOR C109
                      '4dt
                      '4dt
S11 = S011 XOR C110
                      '4dt
S12 = S012 XOR C111
                      '4dt
S13 = S013 XOR C112
                      '4dt
S14 = S014 XOR C113
                      '4dt
S15 = S015 \times C114
C15 =
                      '3dt, C15=Cout
               C115
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Программа проверки системы логических уравнений двоичного сумматора Склянского, Radix-16, 16-ти битного, быстрого, на TurboBasic'e: <a href="https://andserkul.narod.ru/R16PPA16.bas">https://andserkul.narod.ru/R16PPA16.bas</a>

Для 64-битного сумматора Склянского потребуется 4 Radix-16 блока, которые образуют 2-х ступенчатый сумматор Склянского 4х16, или 8 Radix-8 блоков, которые образуют тоже 2-х ступенчатый сумматор Склянского 8х8, но количество входов в наибольших операторах вычисления Р и G будет вдвое меньшим, поэтому, по аппаратным затратам, 64-х битный сумматор Склянского Radix-8 более экономичен, чем 64-х битный сумматор Склянского Radix-16. 64-х битный же двоичный сумматор Склянского Radix-4 16х4 будет иметь три ступени и, поэтому, будет менее быстродействующим, чем сумматор Склянского Radix-8 8х8.

## Литература:

- 1. Kogge-Stone adder. Wikipedia.
- 2. <u>Logical Effort of Higher Valency Adders. David Harris</u>
- 3. <u>Design Space Exploration for Power-Efficient Mixed-Radix Ling Adders. Chung-Kuan Cheng. Computer Science and Engineering Depart. University of California, San Diego.</u>
- 4. Сумматор Склянского, Radix-2, 4-х битный. Куликов А. С.
- 5. <u>Сумматор Склянского, Radix-2, 8-ми битный. Куликов А. С.</u>
- 6. Сумматор Склянского, Radix-2, 16-ти битный. Куликов А. С.
- 7. Сумматор Склянского, Radix-3, 4-х битный. Куликов А. С.
- 8. Сумматор Склянского, Radix-3, 8-ми битный. Куликов А. С.
- 9. Сумматор Склянского, Radix-3, 16-ти битный. Куликов А. С.
- 10. <u>Сумматор Склянского, Radix-4, 4-х битный. Куликов А. С.</u>
- 11. Сумматор Склянского, Radix-4, 8-ми битный. Куликов А. С.
- 12. <u>Сумматор Склянского, Radix-4, 16-ти битный. Куликов А. С.</u>
- 13. <u>Сумматор Склянского, Radix-8, 8-ми битный. Куликов А. С.</u>
- 14. <u>Сумматор Склянского, Radix-8, 16-ти битный. Куликов А. С.</u>

Приложение 1.

## TurboBasic 1.0

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